

Electromagnetic simulations of Toroidal Alfvén Eigenmode (TAE) using GYSELA

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Toroidal Alfvén Eigenmodes (TAEs) are key instabilities in magnetically confined plasmas, due to their interaction with energetic particles and background turbulence [1]. By enhancing energetic ion transport, they could degrade confinement in future devices like ITER [2,3]. While their excitation mechanisms are relatively well understood, their nonlinear saturation —especially the role of zonal flows remains elusive. Furthermore, nonlinear interactions between TAEs and drift-wave microturbulence are not well understood. Some experimental evidence suggests that TAEs may even mitigate turbulence. The understanding of these processes requires global, full-F, flux-driven simulations, as numerous global gyrokinetic studies of TAEs have been performed, but to our knowledge, none have yet used a full-F, flux-driven framework. This approach can unveil unforeseen effects during the nonlinear evolution of TAE modes.

In this study, we present simulations of both antenna-driven and fast ion-driven TAEs using the GYrokinetic SEmi-LAgrangian (GYSELA) code, a global, flux-driven, full-F, semi-Lagrangian framework designed for nonlinear gyrokinetic simulations of plasma turbulence in tokamaks [4]. To investigate the linear excitation and evolution of TAEs, we have solved the electromagnetic gyrokinetic equations. A mixed-variable scheme has been implemented to solve the Ampère equation [5]. This helps in reducing the numerical inaccuracies associated with the parallel vector potential.

The simulation results demonstrate consistent and accurate modeling of both antenna-driven and energetic particle (EP) driven TAEs, with trends that closely align with previously reported ITPA benchmark studies in [6,7]. In the antennadriven scenarios, resonant excitation of m = 3 and m = 4modes for n = 2 TAEs near $r/a \approx 0.5$ with sharp frequency response peak at $\omega_{ant}/\omega_A \approx 0.287$, confirm precise matching with TAE eigenfrequencies as shown in Fig.1(a)-(b). This further validates GYSELA's capability to accurately capture both the radial localization and symmetry of the modes. In EP-driven scenarios, GYSELA accurately reproduces the expected growth rate and frequency scaling with fast-ion temperature (T_f) , showing close agreement with other codes, as illustrated in Fig. 2(a)-(b). Phase-space diagnostics based on energy and canonical toroidal momentum reveal multiple resonances in both linear and nonlinear phases, offering insights into EP-driven mode saturation. A potential signature of zonal flows appears in the radial electric field evolution, likely driven nonlinearly by antenna-excited TAEs, indicating self-generated shear layers critical for regulating turbulence and saturation. Recent works [8,9] further emphasize the pivotal role of zonal flows in the nonlinear saturation of EP-driven modes.

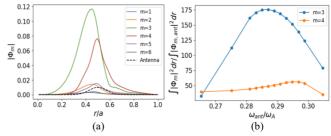


Fig.1: (a) Radial profile of electrostatic plasma potential for n=2 TAE mode. The radial profile of antenna potential is depicted in black-dashed curve. (b) Linear excitation of n=2 TAE at arrange of frequencies near the resonance. The amplitude of plasma potential is integrated in the radial direction and its maximum over a time span is taken.

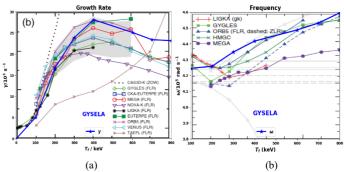


Fig.2: (a) Growth rate of the TAE mode as a function of T_f for the ITPA case. (b) Corresponding TAE frequency variation with T_f showing strong agreement with other established codes.

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